



LegumeLegacy

SS4 Statistical modelling



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**State Secretariat for Education,
Research and Innovation SERI**



UKRI

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Modelling BEF relationships using Diversity-Interactions models and the **DImodels** R package

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Ireland



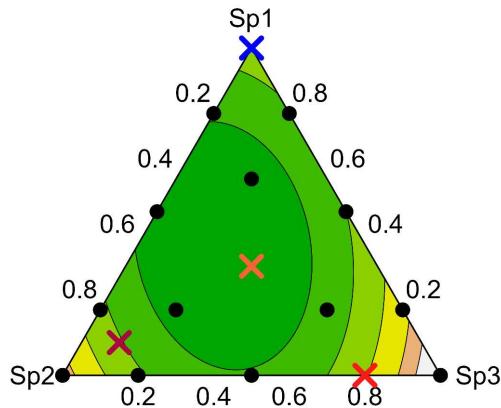
Trinity College Dublin

Coláiste na Tríonóide, Baile Átha Cliath

The University of Dublin

With thanks to Laura Byrne, Rafael Moral, James O'Malley and Rishabh Vishwakarma
who developed some of the material contained in this presentation.

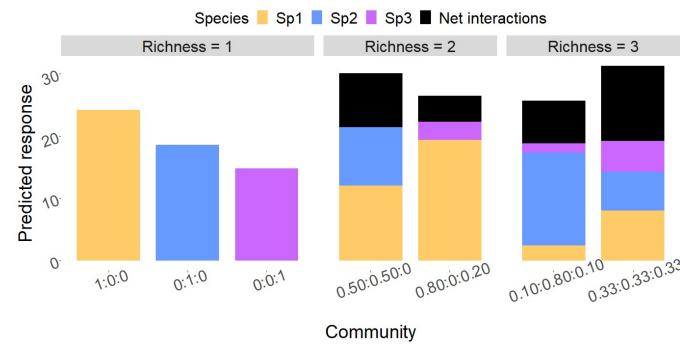
The plan for this training day?



Selecting the best model?

$$y = \sum_{i=1}^s \beta_i p_i + \sum_{\substack{i,j=1 \\ i < j}}^s \delta_{ij} (p_i p_j)^\theta + \varepsilon$$
$$\varepsilon \sim \text{IID } N(0, \sigma^2)$$

Understanding model selection choices?



Model interpretation?

Model communication?

"All models are wrong, but some are useful"

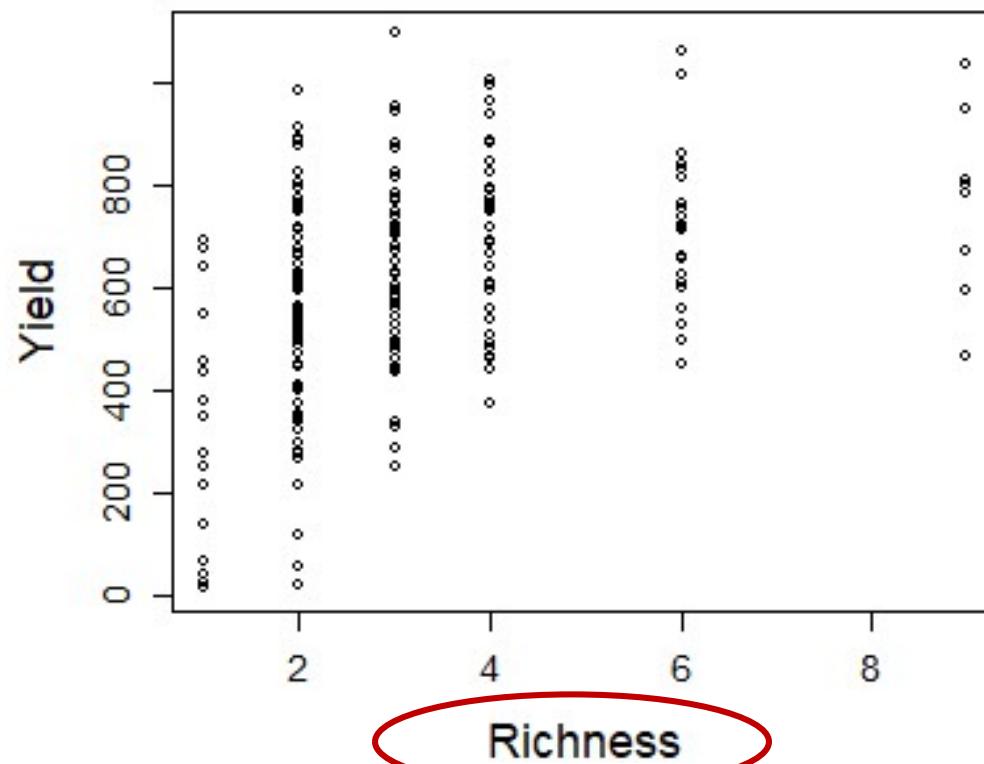
The biodiversity and ecosystem function (BEF) relationship



The biodiversity and ecosystem function (BEF) Relationship

Roscher et al 2004

Jena “dominance” experiment



Non-legume herbs



Legumes



Roscher C, Schumacher J, Baade J, Wilcke W, Gleixner G, Weisser WW, Schmid B, Schulze ED (2004) The role of biodiversity for element cycling and trophic interactions: an experimental approach in a grassland community. *Basic and Applied Ecology*. 2004 5:107-21.

Diversity-Interactions modelling for BEF data

Ecology, 90(8), 2009, pp. 2032–2038
© 2009 by the Ecological Society of America

Diversity–interaction modeling: estimating contributions of species identities and interactions to ecosystem function

L. KIRWAN,^{1,2,7} J. CONNOLLY,³ J. A. FINN,¹ C. BROPHY,^{3,8} A. LÜSCHER,⁴ D. NYFELER,⁴ AND M.-T. SEBASTIA^{5,6}

Journal of Ecology 2013, 101, 344–355

doi: 10.1111/j.1365-2745.12052

An improved model to predict the effects of changing biodiversity levels on ecosystem function

John Connolly^{1*}, Thomas Bell², Thomas Bolger³, Caroline Brophy⁴, Timothee Carnus^{1,5}, John A. Finn⁵, Laura Kirwan⁶, Forest Isbell⁷, Jonathan Levine⁸, Andreas Lüscher⁹, Valentin Picasso¹⁰, Christiane Roscher¹¹, Maria Teresa Sebastia^{12,13}, Matthias Suter^{8,9} and Alexandra Weigelt¹⁴

Received: 9 December 2022 | Accepted: 13 May 2023
DOI: 10.1111/2041-210X.14158

APPLICATION

Methods in Ecology and Evolution
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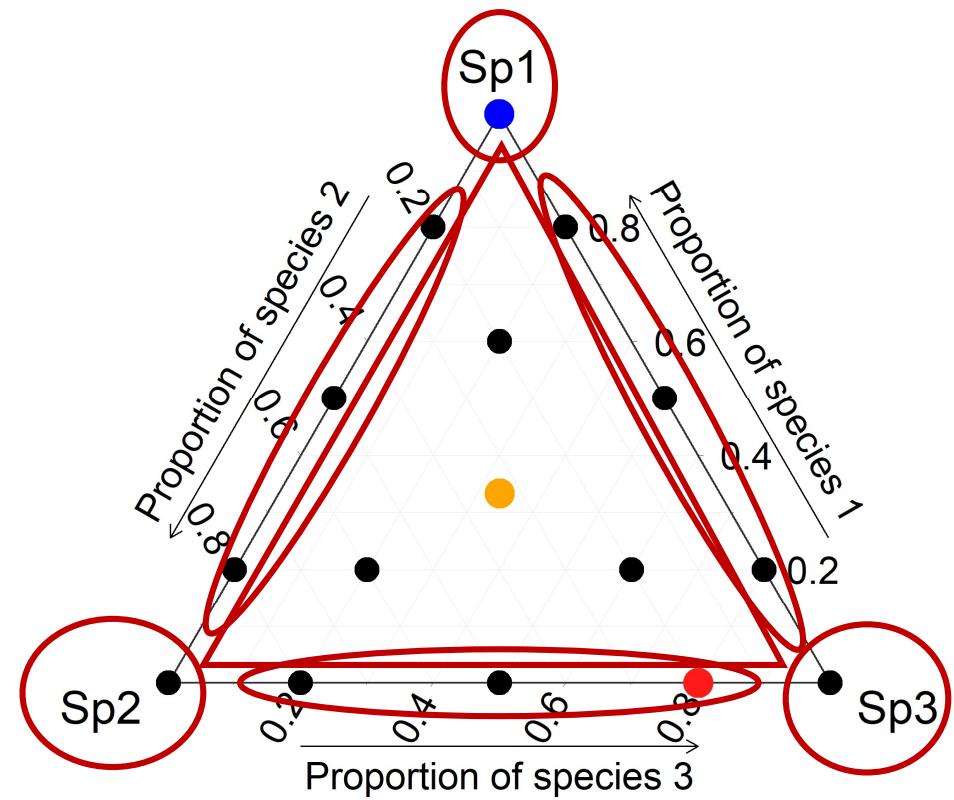
Going beyond richness: Modelling the BEF relationship using species identity, evenness, richness and species interactions via the **DImodels R package**

Rafael A. Moral¹ | Rishabh Vishwakarma² | John Connolly³ | Laura Byrne² | Catherine Hurley¹ | John A. Finn⁴ | Caroline Brophy²

Species biodiversity?

community	richness	p1	p2	p3	response
1	1	1	0	0	24.855
2	1	0	1	0	19.049
3	1	0	0	1	16.292
4	2	0.8	0.2	0	31.529
5	2	0.2	0.8	0	25.102
6	2	0.8	0	0.2	24.615
:	:	:	:	:	:

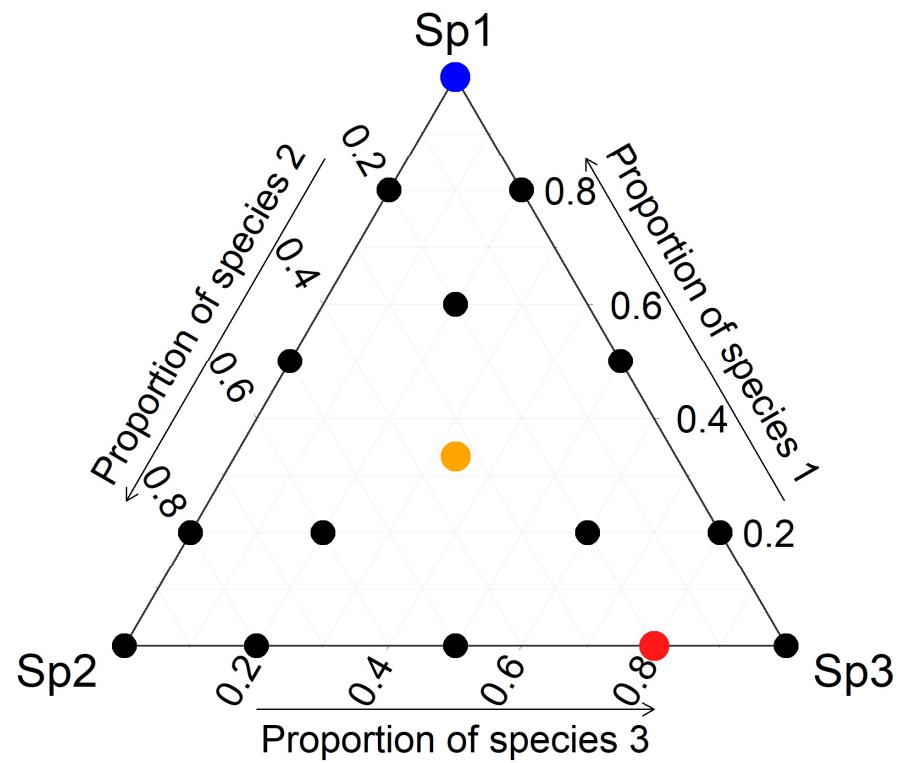
```
install.packages("DImodels")
library(DImodels)
data("sim0")
head(sim0)
```



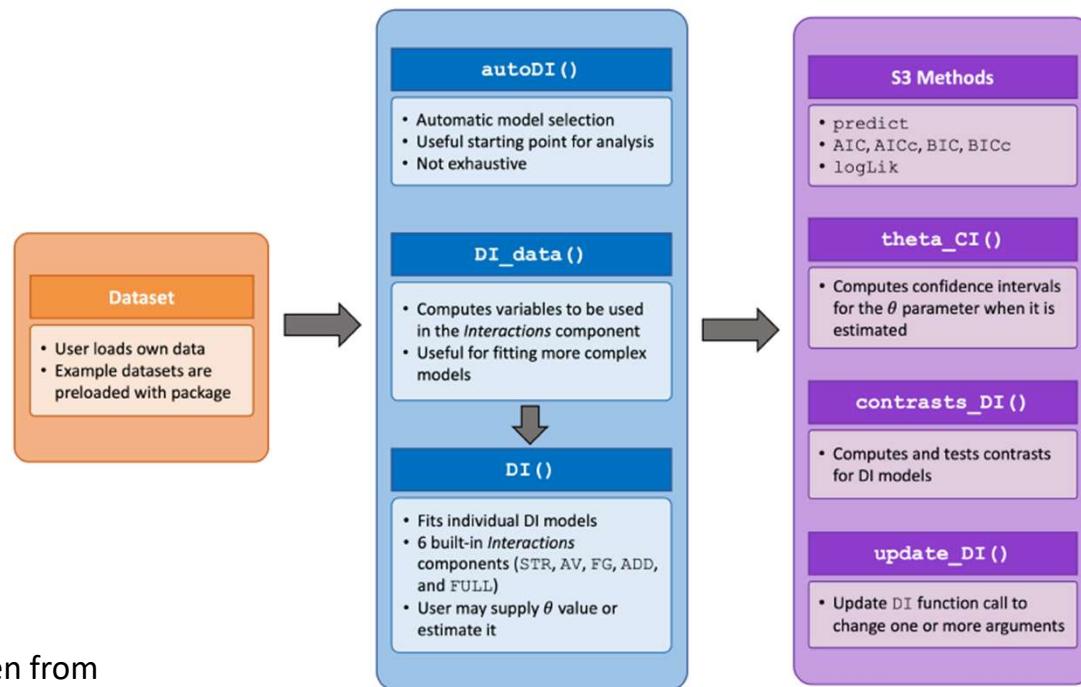
Species biodiversity?

1. Composition – species identity
2. Richness
3. Species proportions

Diversity-Interactions (DI) models can capture all these aspects of species diversity when modelling the BEF relationship



Overview of the DImodels R package



Taken from
Moral et al (2023)
Methods in Ecology and Evolution;
9, 2250-2258.

Additional packages:
DImodelsVis
DImodelsMulti

Example 1

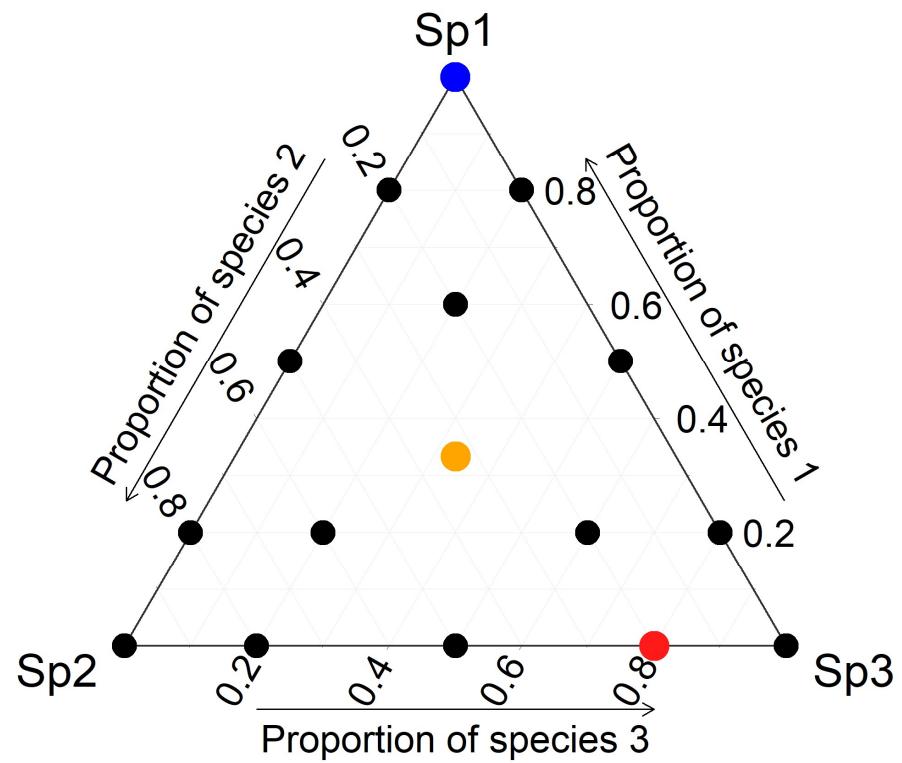
Modelling a 3-species dataset

Moral et al 2023 Methods in Ecology and Evolution; 9, 2250-2258.

Analysing the sim0 dataset

community	richness	p1	p2	p3	response
1	1	1	0	0	24.855
2	1	0	1	0	19.049
3	1	0	0	1	16.292
4	2	0.8	0.2	0	31.529
5	2	0.2	0.8	0	25.102
6	2	0.8	0	0.2	24.615
:	:	:	:	:	:

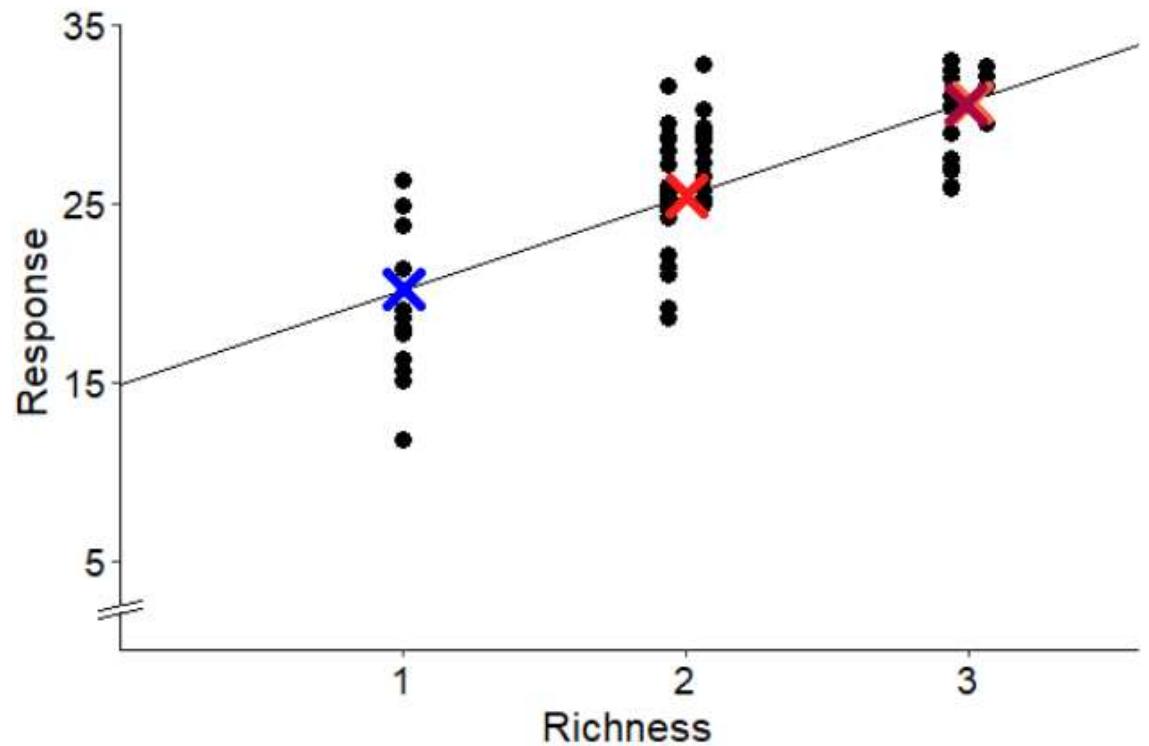
```
install.packages("DImodels")
library(DImodels)
data("sim0")
head(sim0)
```



Analysing the sim0 dataset: simple linear regression

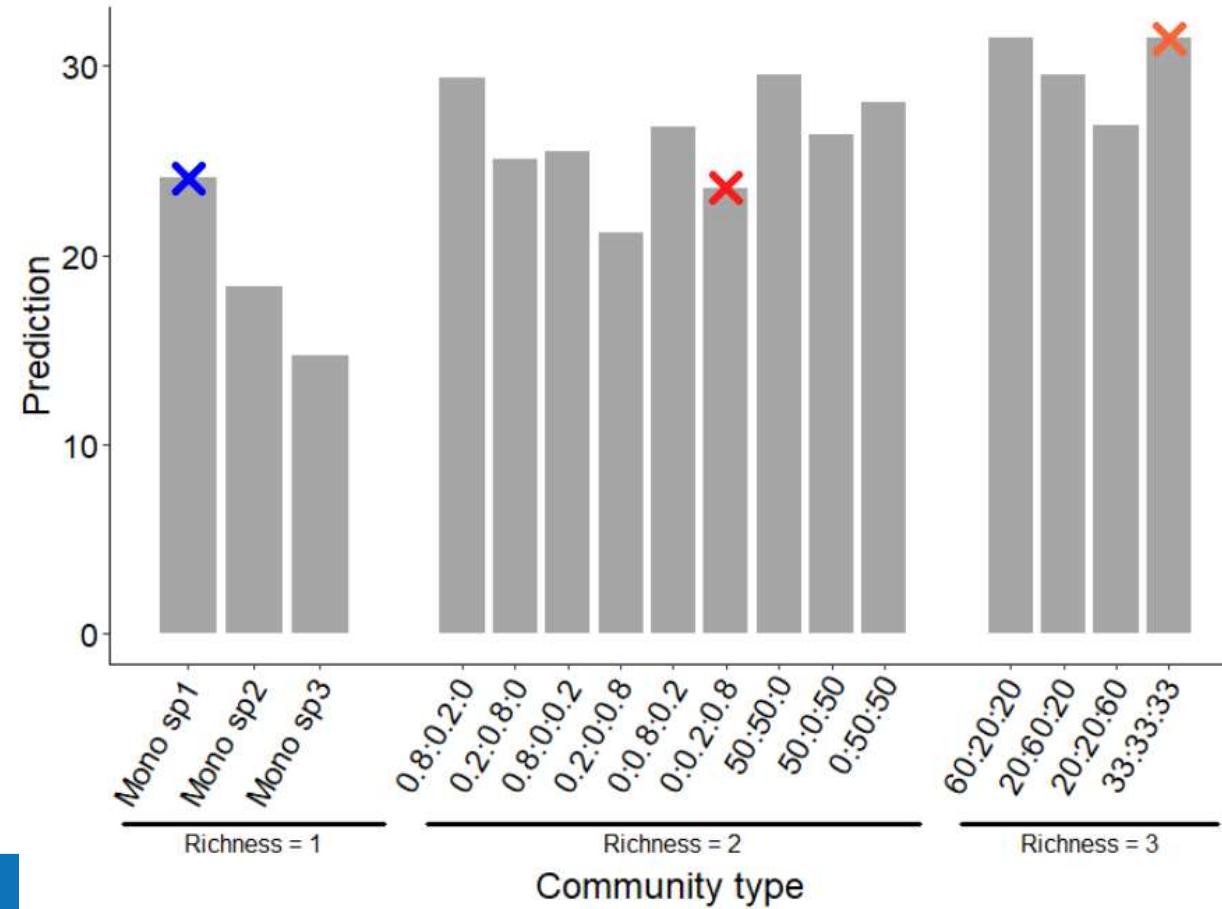
```
m1 <- lm(response ~ richness,  
          data = sim0)  
summary(m1)
```

	Estimate	Std. Error	P-value
Intercept	14.91	1.3781	p < 0.001
richness	5.25	0.6365	p < 0.001



Analysing the sim0 dataset: ANOVA model

```
sim0$communityF <- as.factor(sim0$community)
m2 <- lm(response ~ communityF, data = sim0)
summary(m2)
preds <- predict(m2)
preds[1:16]
```

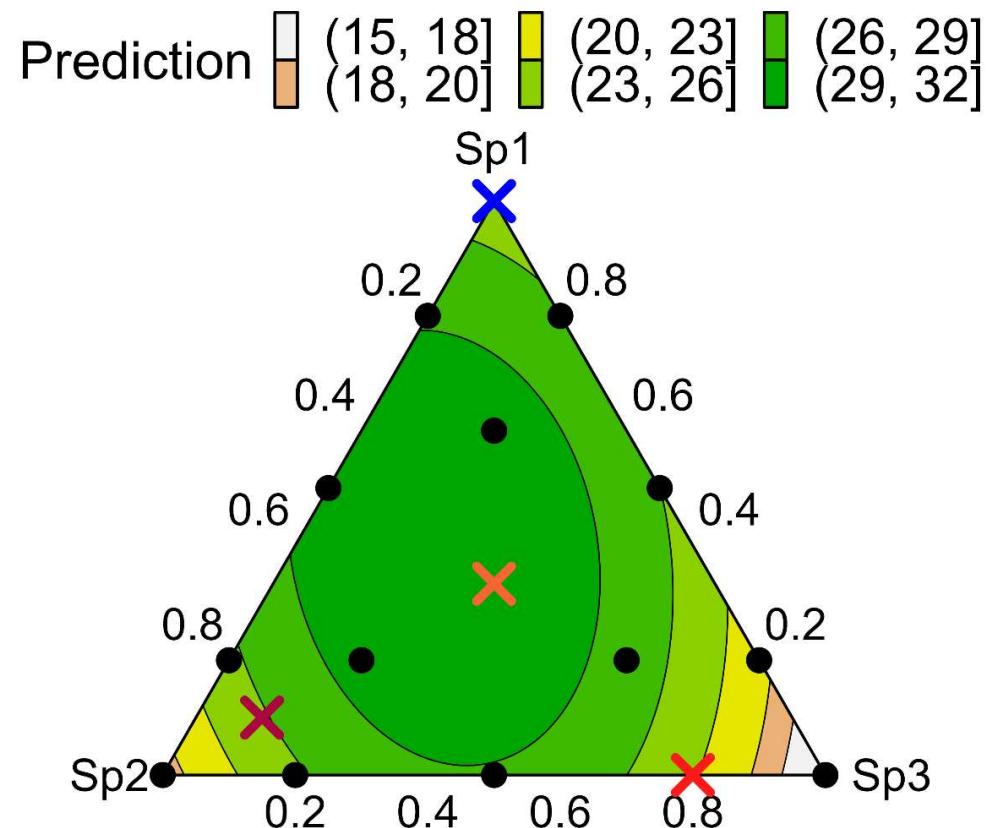


Analysing the sim0 dataset: Diversity-Interactions model

```
m3 <- DI(y = "response", prop = 3:5,
           DImodel = "FULL", data = sim0)
summary(m3)
```

$$y = \sum_{i=1}^3 \beta_i p_i + \sum_{\substack{i,j=1 \\ i < j}}^3 \delta_{ij} p_i p_j + \varepsilon \quad \varepsilon \sim \text{IID } N(0, \sigma^2)$$

Sown prop	Estimate	Std. Error	P-value
p1	24.17	0.7698	
p2	18.62	0.7698	
p3	14.81	0.7698	
p1*p2	34.83	3.5694	p < 0.001
p1*p3	26.14	3.5694	p < 0.001
p2*p3	47.92	3.5694	p < 0.001



Analysing the sim0 dataset: Diversity-Interactions model

```
m3 <- DI(y = "response", prop = 3:5,
           DImodel = "FULL", data = sim0)
summary(m3)
```

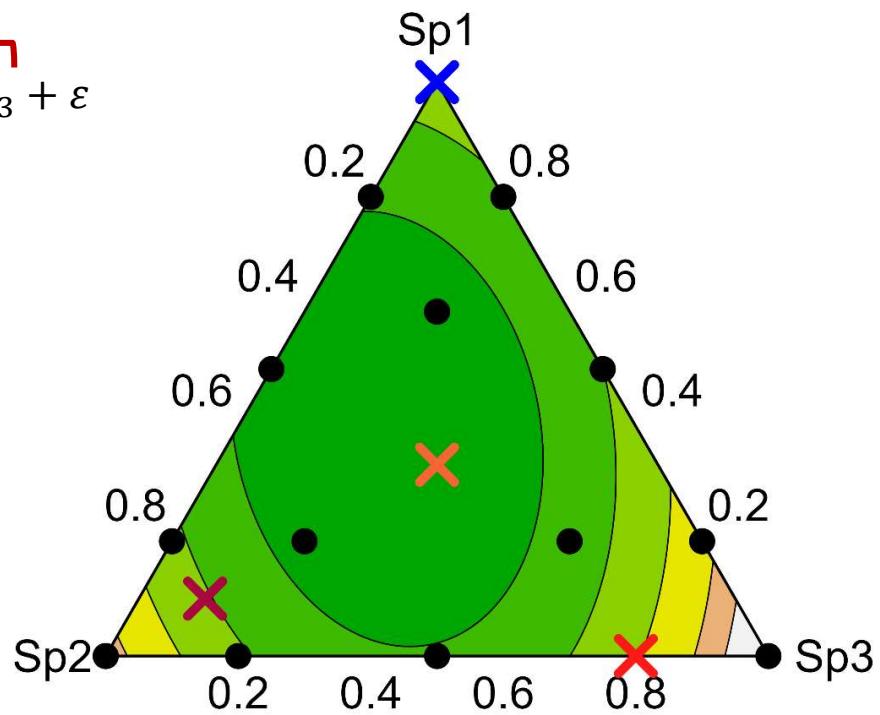
$$y = \beta_1 p_1 + \beta_2 p_2 + \beta_3 p_3 + \delta_{12} p_1 p_2 + \delta_{23} p_2 p_3 + \delta_{13} p_1 p_3 + \varepsilon$$

$$\varepsilon \sim \text{IID } N(0, \sigma^2)$$

Sown prop	Estimate	Std. Error	P-value
p1	24.17	0.7698	
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p1*p3	26.14	3.5694	p < 0.001
p2*p3	47.92	3.5694	p < 0.001

Prediction

	(15, 18]		(20, 23]		(26, 29]
	(18, 20]		(23, 26]		(29, 32]



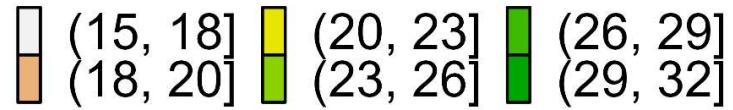
Analysing the sim0 dataset: Diversity-Interactions model

$$y = \sum_{i=1}^3 \beta_i p_i + \sum_{\substack{i,j=1 \\ i < j}}^3 \delta_{ij} p_i p_j + \varepsilon$$

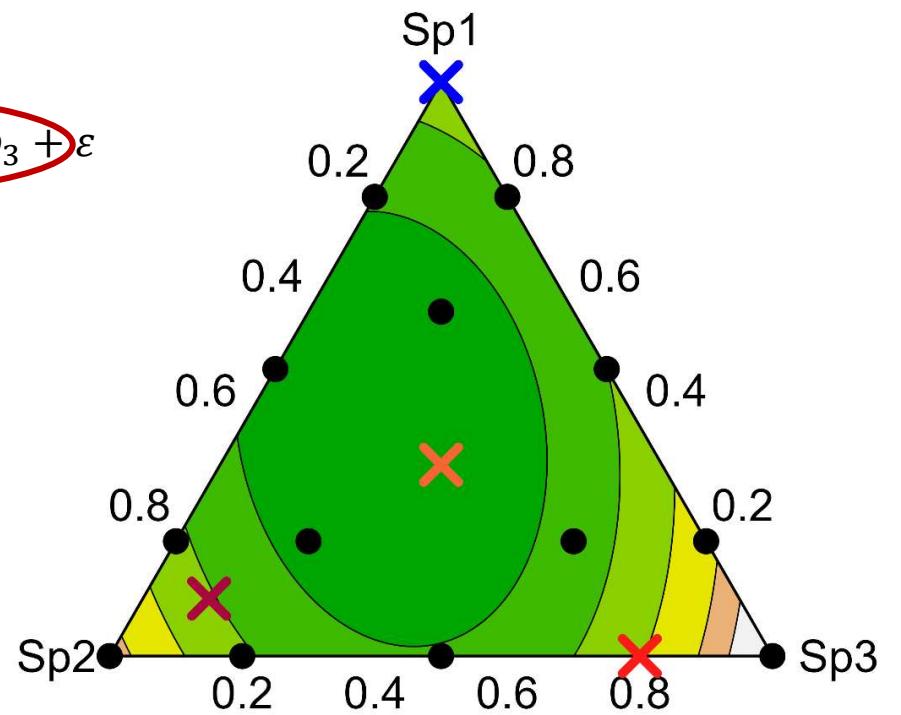
$$\varepsilon \sim \text{IID } N(0, \sigma^2)$$

Prediction

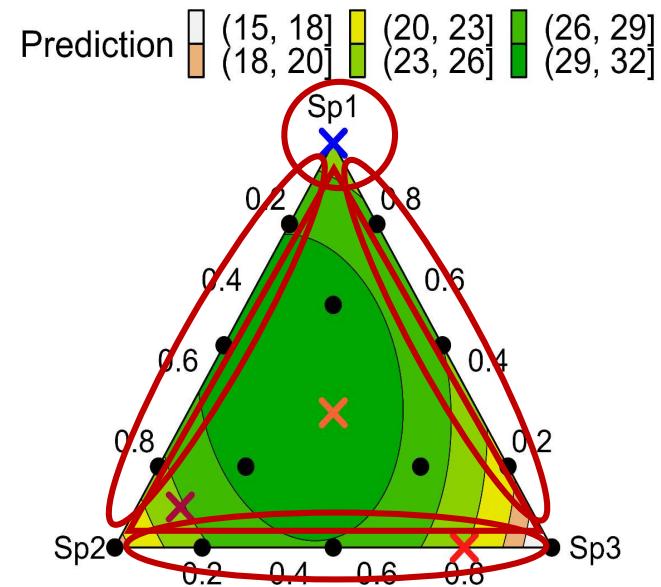
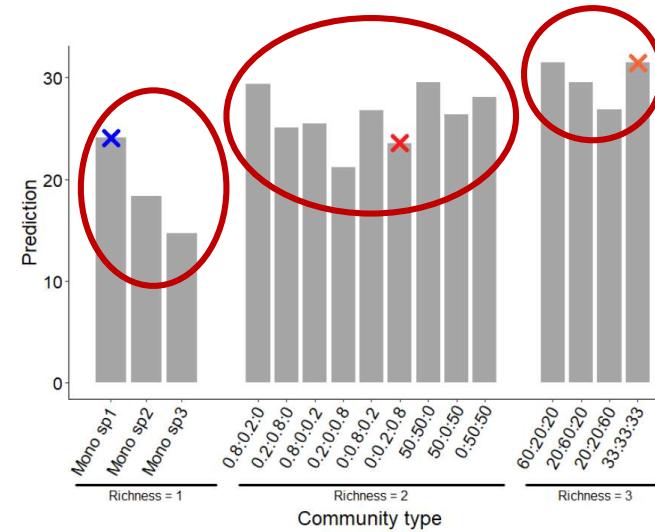
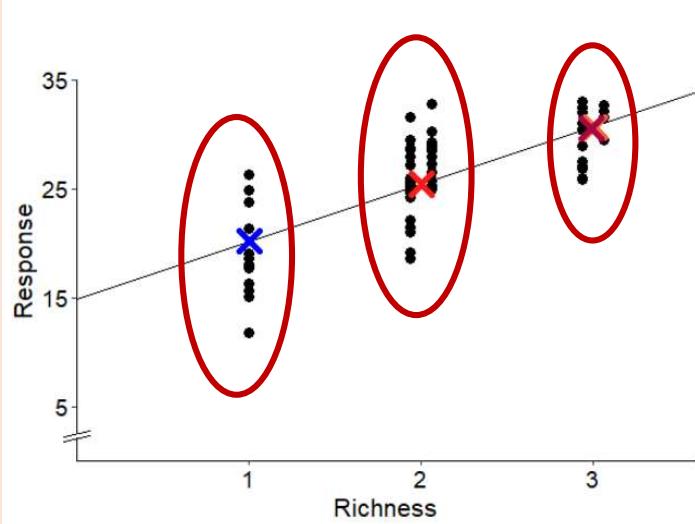
$$y = \beta_1 p_1 + \beta_2 p_2 + \beta_3 p_3 + \delta_{12} p_1 p_2 + \delta_{23} p_2 p_3 + \delta_{13} p_1 p_3 + \varepsilon$$



Sown prop	Estimate	Std. Error	P-value
p1	24.17	0.7698	
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The strength of DI models



Example 2

Modelling a 4-species BEF dataset



Now, you will work through the tutorial and later we will come back to this presentation.

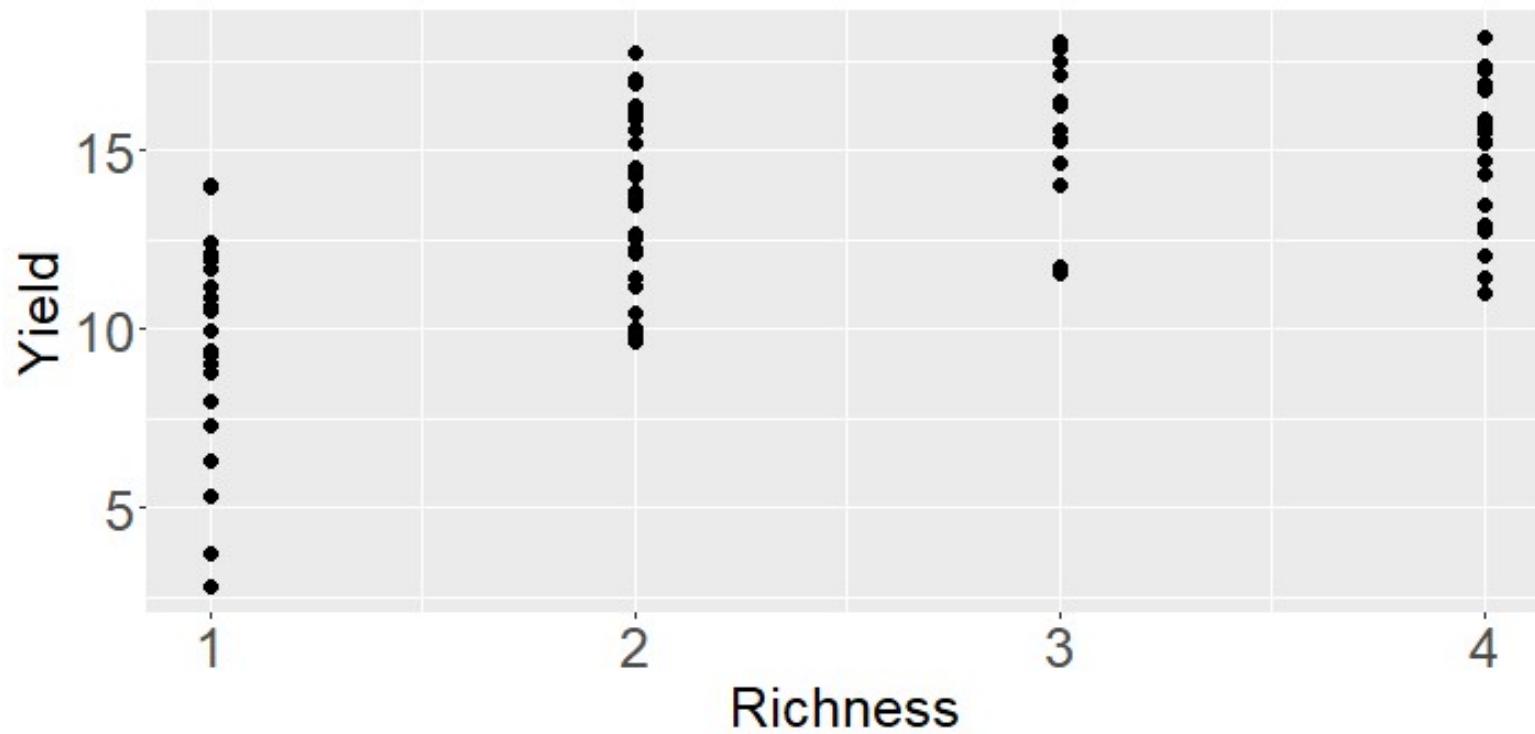
Simulated dataset

- Filename: Dataset_4species_simulated.csv
- Simulated assuming a biodiversity and ecosystem function (BEF) experiment
- Four grassland species (species 1 and 2 grasses, species 3 and 4 legumes), let's call them G1, G2, L1 and L2.
- Species diversity and nitrogen fertiliser treatments manipulated across plots
- Total of 100 plots (50 at low and 50 at regular N)
- Yield of each plot over a growing season was recorded

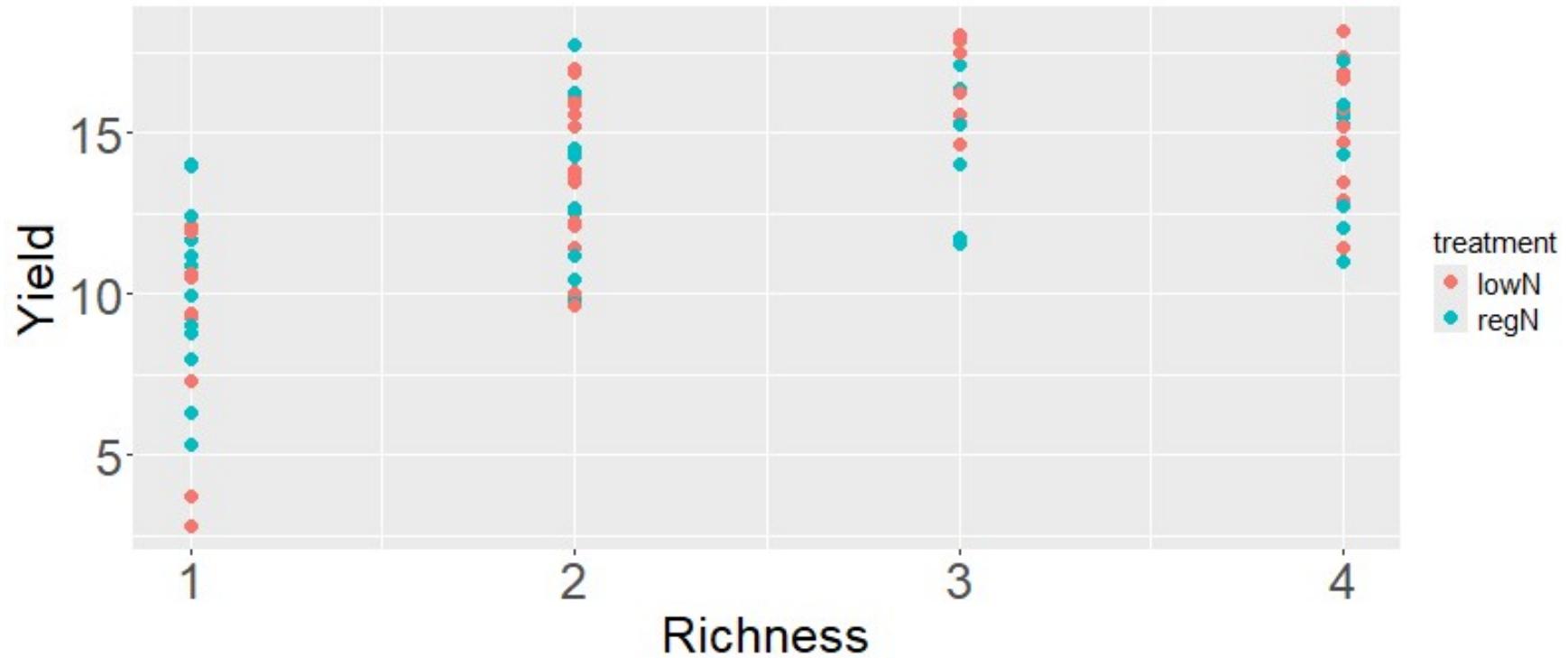
Example 2 continued
Modelling a 4-species BEF dataset

Explore the data graphically

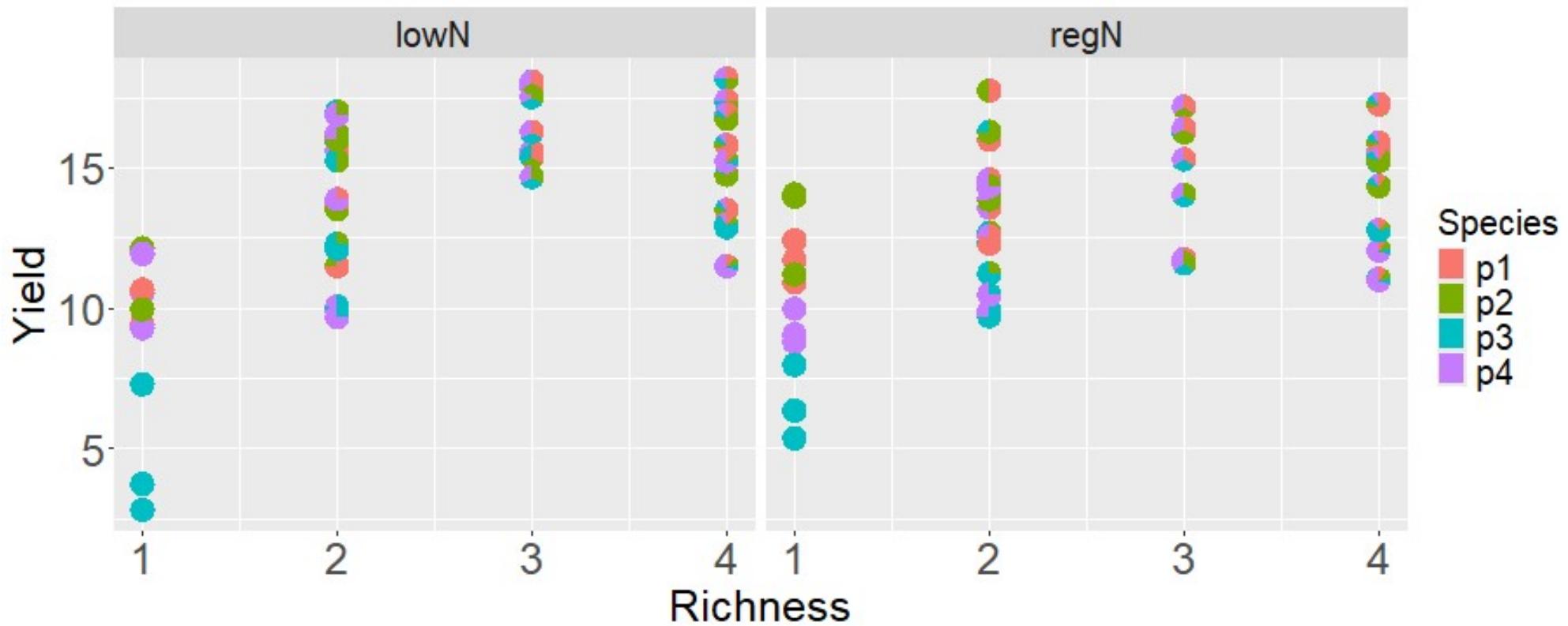
Explore the data



Explore the data



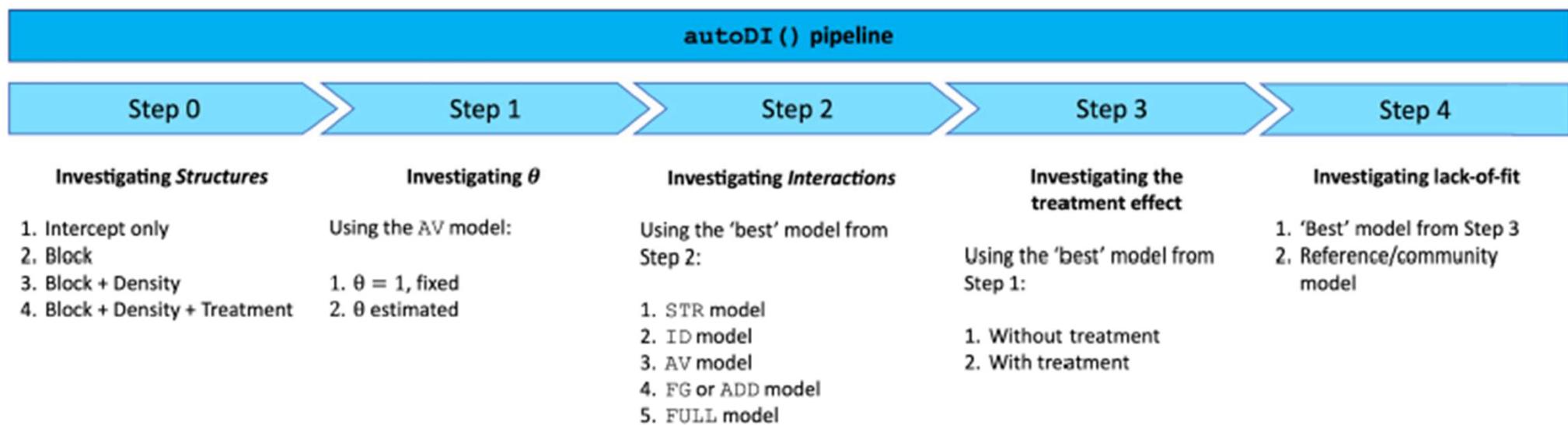
Explore the data



Example 2 continued
Modelling a 4-species BEF dataset

Initial model selection using autoDI

Using autoDI for model selection



Taken from
Moral et al (2023)
Methods in Ecology and Evolution; 9, 2250-2258.

Using autoDI for model selection

Sequential analysis: Investigating only non-diversity experimental design structures

	model	Resid.	Df	Resid.	SSq	Resid.	MSq	Df	SSq	F	Pr(>F)
1	Intercept only		99	1029.603		10.400					
2	treat		98	1023.218		10.441	1	6.3847	0.6115	0.4361	

For a scientific presentation, don't give R output like this!

Models fitted?

Using autoDI for model selection

Step 1: Investigating whether theta is equal to 1 or not for the AV model, including all available structures

Theta estimate: 1.0017

Selection using F tests

Description												
DI Model 1 Average interactions 'AV' DImodel with treatment												
DI Model 2 Average interactions 'AV' DImodel with treatment, estimating theta												
DI_model	treat	estimate_theta	Resid.	Df	Resid.	SSq	Resid.	MSq	Df	SSq	F	Pr(>F)
DI Model 1	AV	'treatF'		FALSE	94	219.8445		2.3388				
DI Model 2	AV	'treatF'		TRUE	93	219.8431		2.3639	1	0.0015	6e-04	0.9802

The test concludes that theta is not significantly different from 1.

Models fitted?

Using autoDI for model selection

Step 2: Investigating the interactions

Since 'Ftest' was specified as selection criterion and functional groups were specified, dropping the ADD model as it is not nested within the FG model.

Selection using F tests

```
Description
DI Model 1 Structural 'STR' DImodel with treatment
DI Model 2 Species identity 'ID' DImodel with treatment
DI Model 3 Average interactions 'AV' DImodel with treatment
DI Model 4 Functional group effects 'FG' DImodel with treatment
DI Model 5 Separate pairwise interactions 'FULL' DImodel with treatment
```

Models fitted?

DI_model	treat	estimate_theta	Resid.	Df	Resid.	SSq	Resid.	MSq	Df	SSq	F	Pr(>F)
DI Model 1	STR	'treatF'	FALSE	98	1023.2180	10.4410						
DI Model 2	ID	'treatF'	FALSE	95	739.1527	7.7806	3	284.0653	45.5645	<0.0001		
DI Model 3	AV	'treatF'	FALSE	94	219.8445	2.3388	1	519.3082	249.8937	<0.0001		
DI Model 4	FG	'treatF'	FALSE	92	190.8205	2.0741	2	29.024	6.9833	0.0015		
DI Model 5	FULL	'treatF'	FALSE	89	184.9523	2.0781	3	5.8682	0.9413	0.4243		

Selected model: Functional group effects 'FG' DImodel with treatment

Using autoDI for model selection

Step 3: Investigating the treatment effect

Selection using F tests

	Description	Models fitted?
DI Model 1	Functional group effects 'FG' DImodel	
DI Model 2	Functional group effects 'FG' DImodel with treatment	
<hr/>		
DI_model	treat estimate_theta Resid. Df Resid. SSq Resid. MSq Df SSq F Pr(>F)	
DI Model 1	FG none FALSE 93 197.2052 2.1205	
DI Model 2	FG 'treatF' FALSE 92 190.8205 2.0741 1 6.3847 3.0783 0.0827	

Selected model: Functional group effects 'FG' DImodel

Using autoDI for model selection

Step 4: Comparing the final selected model with the reference (community) model
'community' is a factor with 31 levels, one for each unique set of proportions.

	model	Resid.	Df	Resid.	SSq	Resid.	MSq	Df	SSq	F	Pr(>F)
DI Model 1	Selected		93	197.2052		2.1205					
DI Model 2	Reference		69	150.9661		2.1879	24	46.2392	0.8806	0.6251	

autoDI is limited in terms of model selection. Exercise caution when choosing your final model.

Models fitted?

Where are we at after using autoDI?

- Theta set to 1
- FG model for species interactions
 - Grass-legume, grass-grass, legume-legume,
- No effect of N fertiliser

Term	Estimate	Std. Error	P-value
p1_ID	10.9	0.483	<0.001
p2_ID	12.0	0.483	<0.001
p3_ID	6.2	0.483	<0.001
p4_ID	9.5	0.483	<0.001
FG_bfg_GL	20.8	1.427	<0.001
FG_wfg_G	17.6	2.871	<0.001
FG_wfg_L	9.0	2.871	0.002

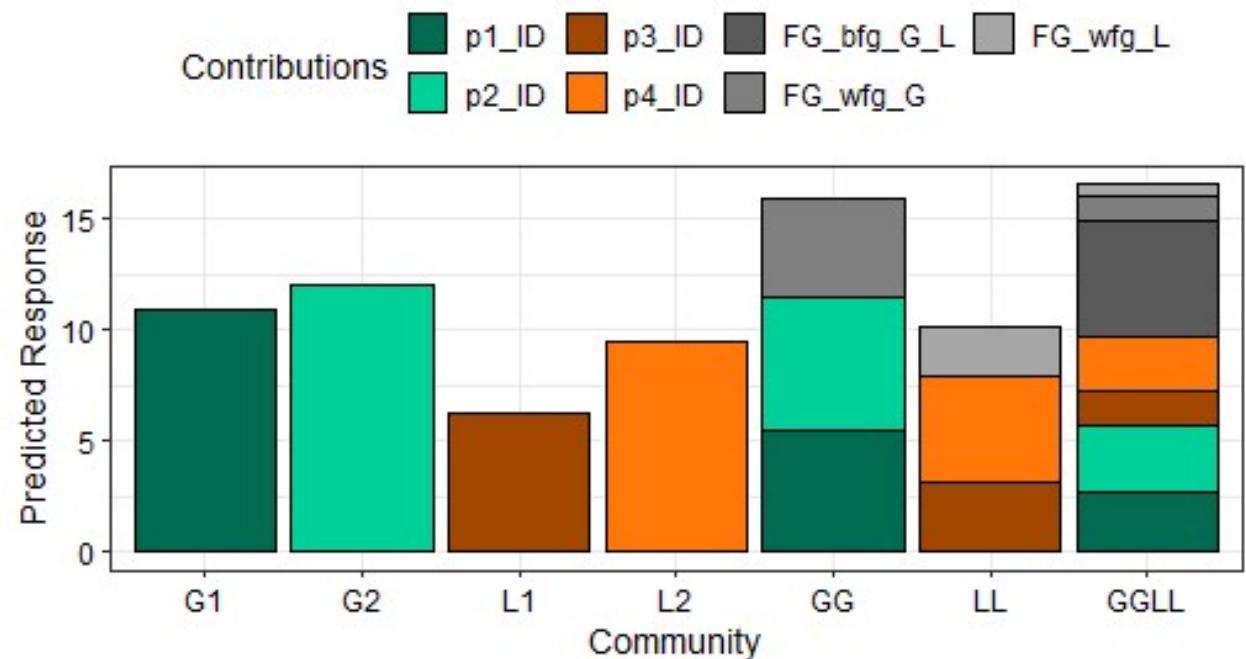
$$y = \sum_{i=1}^4 \beta_i p_i + \delta_{GL} \sum_{\substack{i \in \{1,2\} \\ j \in \{3,4\}}} p_i p_j + \delta_{GG}(p_1 p_2) + \delta_{LL}(p_3 p_4) + \varepsilon \quad \varepsilon \sim \text{IID } N(0, \sigma^2)$$

$$y = \beta_1 p_1 + \beta_2 p_2 + \beta_3 p_3 + \beta_4 p_4 + \delta_{GL}(p_1 p_3 + p_1 p_4 + p_2 p_3 + p_2 p_4) + \delta_{GG}(p_1 p_2) + \delta_{LL}(p_3 p_4) + \varepsilon$$

Matrix notation?

Where are we at after using autoDI?

- Theta set to 1
- FG model for species interactions
 - Grass-grass, legume-legume, grass-legume
- No effect of treatment

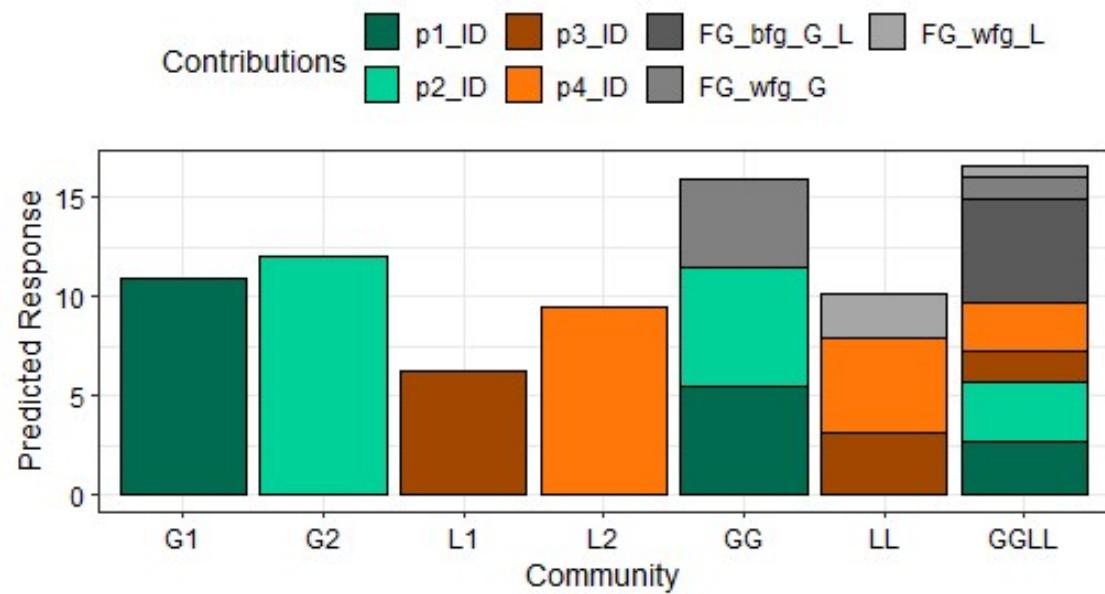


Mixtures are equi-proportional here

Where are we at after using autoDI?

Term	Estimate	Std. Error	P-value
p1_ID	10.9	0.483	<0.001
p2_ID	12.0	0.483	<0.001
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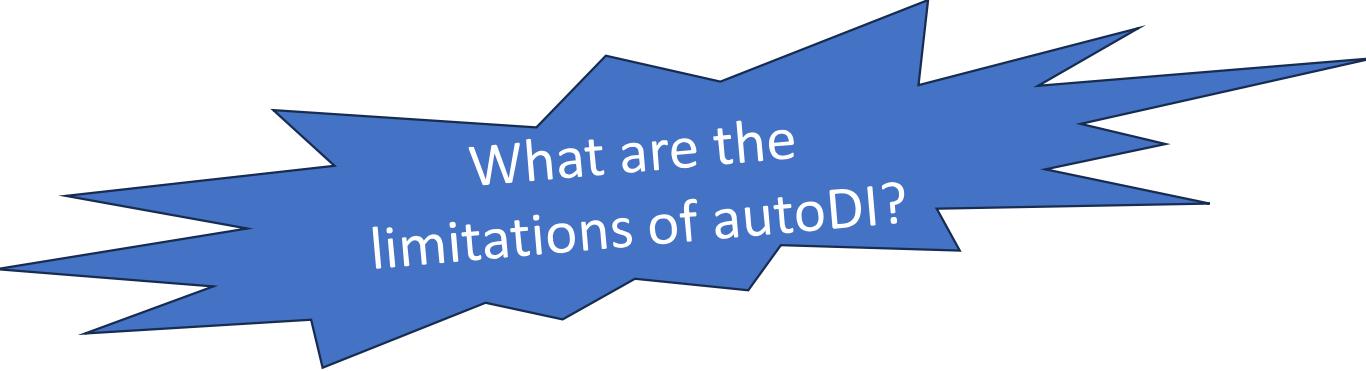
Predicted yield for G1?
For G1 = 0.5, G2 = 0.5?
Do these change by N level?



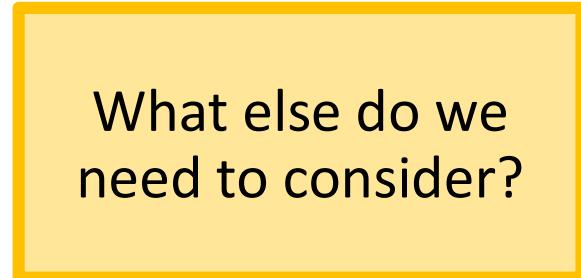
Where are we at after using autoDI?

- Theta set to 1
- FG model for species interactions
 - Grass-grass, legume-legume, grass-legume
- No effect of treatment

autoDI is limited in terms of model selection. Exercise caution when choosing your final model.



What are the
limitations of autoDI?



What else do we
need to consider?

Example 2 continued
Modelling a 4-species BEF dataset

Deep model selection investigation

Does nitrogen affect the BEF relationship?

So far, the nitrogen treatment has only been tested as an additive factor:

$$y = \sum_{i=1}^4 \beta_i p_i + \delta_{GL} \sum_{\substack{i \in \{1,2\} \\ j \in \{3,4\}}} p_i p_j + \delta_{GG}(p_1 p_2) + \delta_{LL}(p_3 p_4) + \alpha X_{rN} + \varepsilon$$

X_{rN} is a dummy variable equal to 1 for regular N and 0 for low N

How else might nitrogen be modelled?

Crossing N with all other model terms

```
DI(y = "response", prop = c("p1", "p2", "p3", "p4"),
  FG = c("G", "G", "L", "L"), DImodel = "FG",
  extra_formula = ~ p1: treatF + p2: treatF + p3: treatF + p4: treatF
  + bfg_G_L: treatF + wfg_G: treatF + wfg_L: treatF,
  data = data1)
```

Crossing N with all other model terms

Sown prop	lowN est	regN est
p1_ID	9.99	11.77
p2_ID	11.33	12.68
p3_ID	5.62	6.85
p4_ID	9.65	9.31
FG_bfg_GL	26.98	14.64
FG_wfg_GG	14.65	20.59
FG_wfg_LL	10.38	7.72

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)	
p1_ID	11.7747	0.5873	20.050	< 2e-16	***
p2_ID	12.6753	0.5873	21.583	< 2e-16	***
p3_ID	6.8511	0.5873	11.666	< 2e-16	***
p4_ID	9.3053	0.5873	15.845	< 2e-16	***
FG_bfg_G_L	14.6371	1.7352	8.436	6.93e-13	***
FG_wfg_G	20.5948	3.4923	5.897	7.08e-08	***
FG_wfg_L	7.7236	3.4923	2.212	0.0296	*
`p1:treatFlowN`	-1.7875	0.8305	-2.152	0.0342	*
`treatFlowN:p2`	-1.3482	0.8305	-1.623	0.1082	
`treatFlowN:p3`	-1.2286	0.8305	-1.479	0.1427	
`treatFlowN:p4`	0.3427	0.8305	0.413	0.6809	
`treatFlowN:bfg_G_L`	12.3432	2.4539	5.030	2.65e-06	***
`treatFlowN:wfg_G`	-5.9494	4.9388	-1.205	0.2316	
`treatFlowN:wfg_L`	2.6524	4.9388	0.537	0.5926	

For a scientific presentation, don't give R output like this!

Model selection

- Reduce the nitrogen interaction terms in the model, removing one non-significant term at a time
- Final model: N crossed with p1, p2 and the grass-legume interaction term

Coefficients:

p1_ID
p2_ID
p3_ID
p4_ID
FG_bfg_G_L
FG_wfg_G
FG_wfg_L
`p1:treatFlowN`
`treatFlowN:p2`
~~`treatFlowN:p3`~~
~~`treatFlowN:p4`~~
~~`treatFlowN:bfg_G_L`~~
~~`treatFlowN:wfg_G`~~
~~`treatFlowN:wfg_L`~~

Example 2 continued
Modelling a 4-species BEF dataset

Final model equation, different
parameterisations and diagnostics

Final model coefficient estimates

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)	
p1_ID	11.9830	0.5592	21.427	< 2e-16	***
p2_ID	12.8836	0.5592	23.038	< 2e-16	***
p3_ID	6.2368	0.4158	15.001	< 2e-16	***
p4_ID	9.4766	0.4158	22.794	< 2e-16	***
FG_bfg_G_L	14.9219	1.5792	9.449	4.00e-15	***
FG_wfg_G	17.6201	2.4723	7.127	2.46e-10	***
FG_wfg_L	9.0498	2.4723	3.660	0.000424	***
`p1:treatFlowN`	-2.2042	0.7481	-2.947	0.004091	**
`treatFlowN:p2`	-1.7648	0.7481	-2.359	0.020475	*
`treatFlowN:bfg_G_L`	11.7736	1.9848	5.932	5.48e-08	***

Term	Low N Est	Reg N Est
p1	9.78	11.98
p2	11.12	12.88
p3	6.23	6.23
p4	9.48	9.48
FG_bfg_GL	26.70	14.92
FG_wfg_G	17.62	17.62
FG_wfg_L	9.05	9.05

Different parameterisations?

Final model coefficient estimates

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)	
p3	6.2368	0.4158	15.001	< 2e-16	***
p4	9.4766	0.4158	22.794	< 2e-16	***
wfg_G	17.6201	2.4723	7.127	2.46e-10	***
wfg_L	9.0498	2.4723	3.660	0.000424	***
p1:treatFlowN	9.7788	0.5592	17.486	< 2e-16	***
p1:treatFregN	11.9830	0.5592	21.427	< 2e-16	***
treatFlowN:p2	11.1188	0.5592	19.882	< 2e-16	***
treatFregN:p2	12.8836	0.5592	23.038	< 2e-16	***
treatFlowN:bfg_G_L	26.6955	1.5792	16.905	< 2e-16	***
treatFregN:bfg_G_L	14.9219	1.5792	9.449	4.00e-15	***

Term	Low N Est	Reg N Est
p1	9.78	11.98
p2	11.12	12.88
p3	6.23	6.23
p4	9.48	9.48
FG_bfg_GL	26.70	14.92
FG_wfg_G	17.62	17.62
FG_wfg_L	9.05	9.05

Others?

Final model coefficient estimates

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)	
p1	9.7788	0.5592	17.486	< 2e-16	***
p2	11.1188	0.5592	19.882	< 2e-16	***
p3	6.2368	0.4158	15.001	< 2e-16	***
p4	9.4766	0.4158	22.794	< 2e-16	***
bfg_G_L	26.6955	1.5792	16.905	< 2e-16	***
wfg_G	17.6201	2.4723	7.127	2.46e-10	***
wfg_L	9.0498	2.4723	3.660	0.000424	***
p1:regN	2.2042	0.7481	2.947	0.004091	**
p2:regN	1.7648	0.7481	2.359	0.020475	*
bfg_G_L:regN	-11.7736	1.9848	-5.932	5.48e-08	***

Term	Low N Est	Reg N Est
p1	9.78	11.98
p2	11.12	12.88
p3	6.23	6.23
p4	9.48	9.48
FG_bfg_GL	26.70	14.92
FG_wfg_G	17.62	17.62
FG_wfg_L	9.05	9.05

Which parameterisation do you prefer?

Model equation

Let: p_i = sown proportion of species i

$$FG_bfg_GL = p_1p_3 + p_1p_4 + p_2p_3 + p_2p_4$$

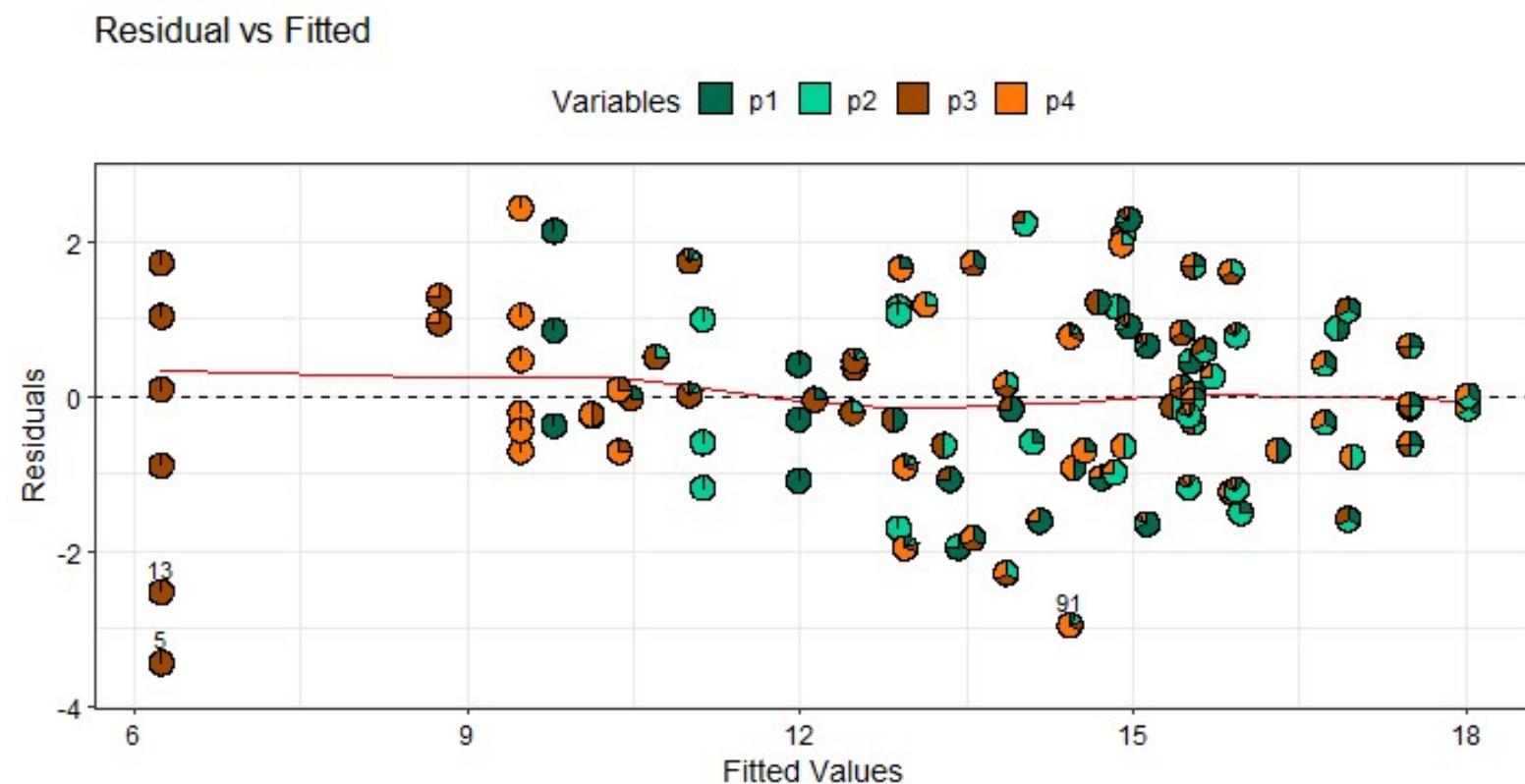
X_{rN} = 1 for regular N and 0 for low N

$$\begin{aligned} y = & \beta_1 p_1 + \beta_2 p_2 + \beta_3 p_3 + \beta_4 p_4 + \delta_{GL}(FG_bfg_GL) + \delta_{GG}(p_1 p_2) + \delta_{LL}(p_3 p_4) \\ & + \beta_{1rN} p_1 X_{rN} + \beta_{2rN} p_2 X_{rN} + \delta_{GL_rN}(FG_bfg_GL) X_{rN} + \varepsilon \end{aligned}$$

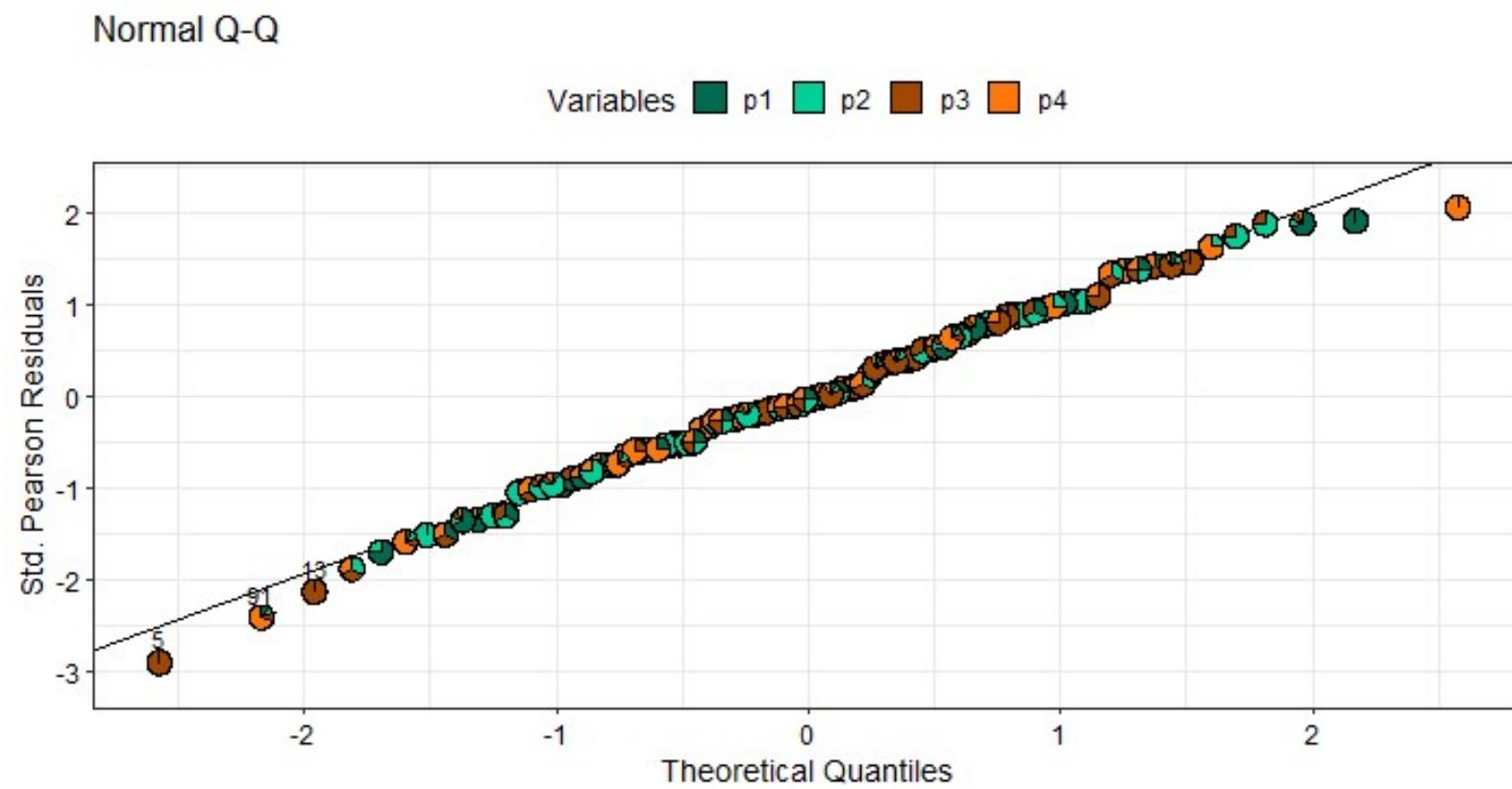
$$\varepsilon \sim \text{IID } N(0, \sigma^2)$$

Matrix
notation?

Final model diagnostics



Final model diagnostics



Example 2 continued
Modelling a 4-species BEF dataset

Predicting from the final model

Predicting from the model

- Grass 1 monoculture low N

$$\hat{y} = 9.78$$

- Grass 1 monoculture regular N

$$\hat{y} = 9.78 + 2.20 = 11.98$$

- Equi-prop 4-species mix low N

$$\begin{aligned}\hat{y} = 9.78 \times 0.25 + 11.12 \times 0.25 + 6.24 \times 0.25 + 9.48 \times 0.25 \\ + 26.70 \times 0.25 + 17.62 \times 0.0625 + 9.05 \times 0.0625 = 17.49\end{aligned}$$

- Equi-prop 4-species mix regular N

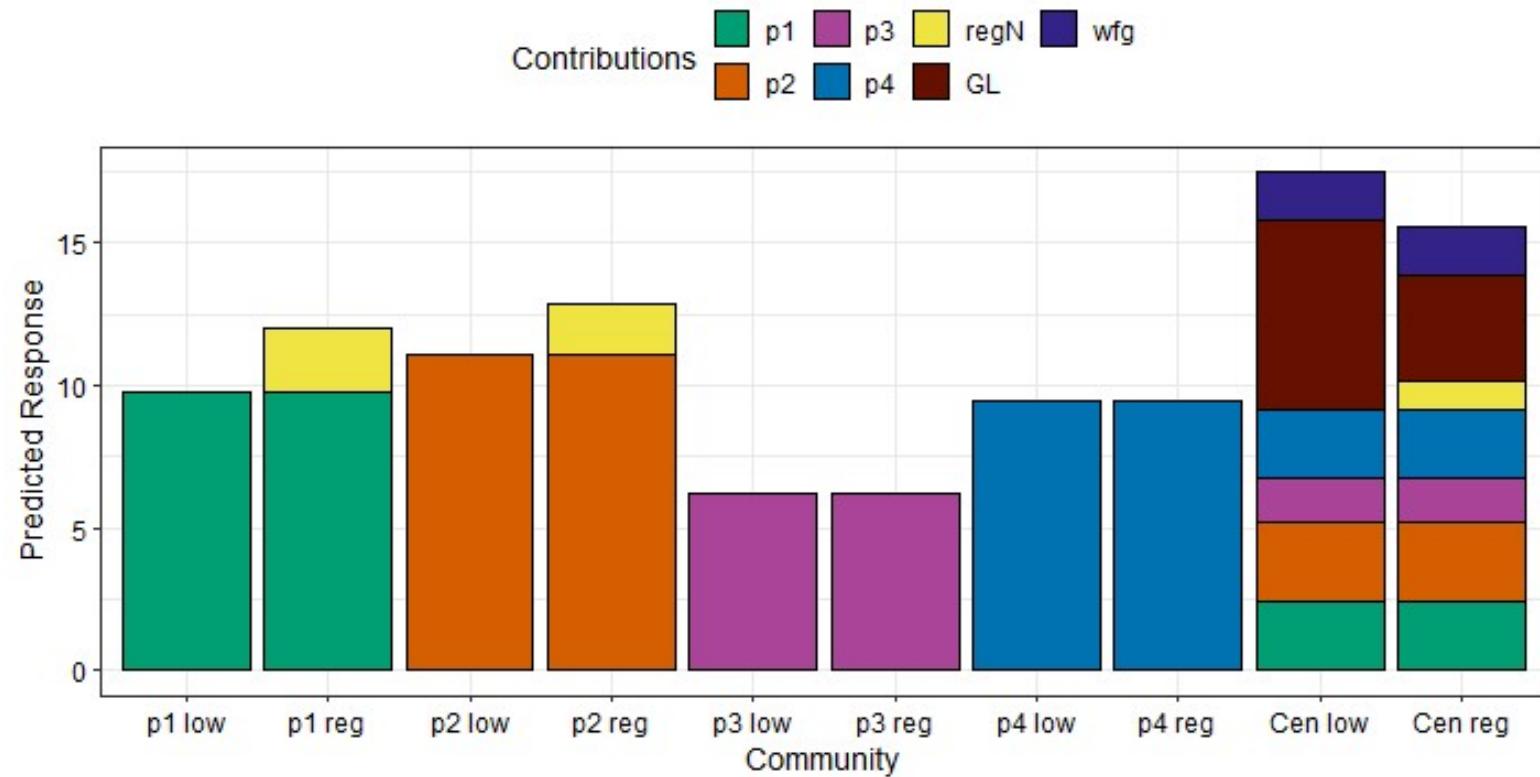
$$\hat{y} = 17.49 + 2.20 \times 0.25 + 1.76 \times 0.25 - 11.77 \times 0.25 = 15.54$$

Term	Estimate
p1_ID	9.78
p2_ID	11.12
p3_ID	6.24
p4_ID	9.48
FG_bfg_G_L	26.70
FG_wfg_G	17.62
FG_wfg_L	9.05
p1:regN	2.20
p2:regN	1.76
bfg_G_L:regN	-11.77

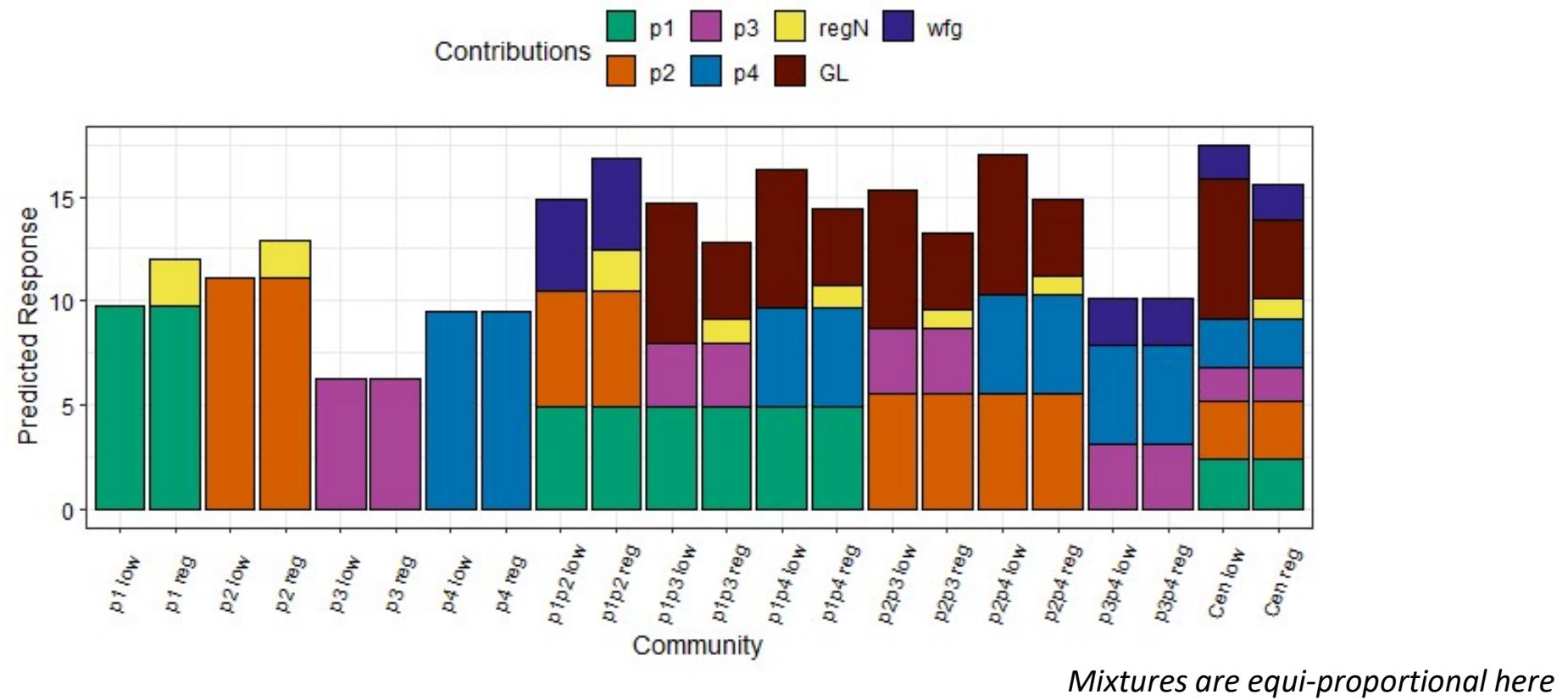
Example 2 continued
Modelling a 4-species BEF dataset

Final model interpretation

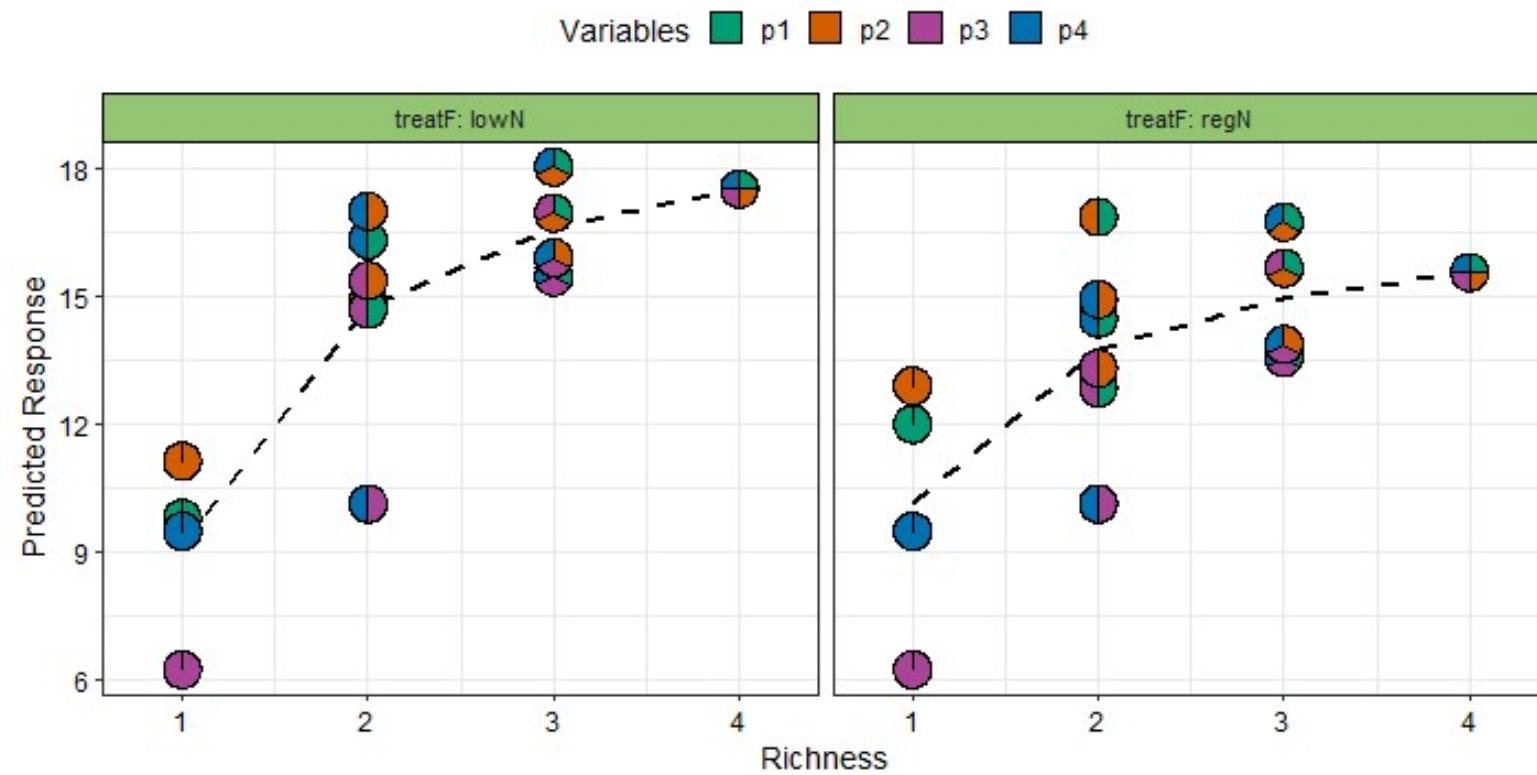
Interpreting the final model



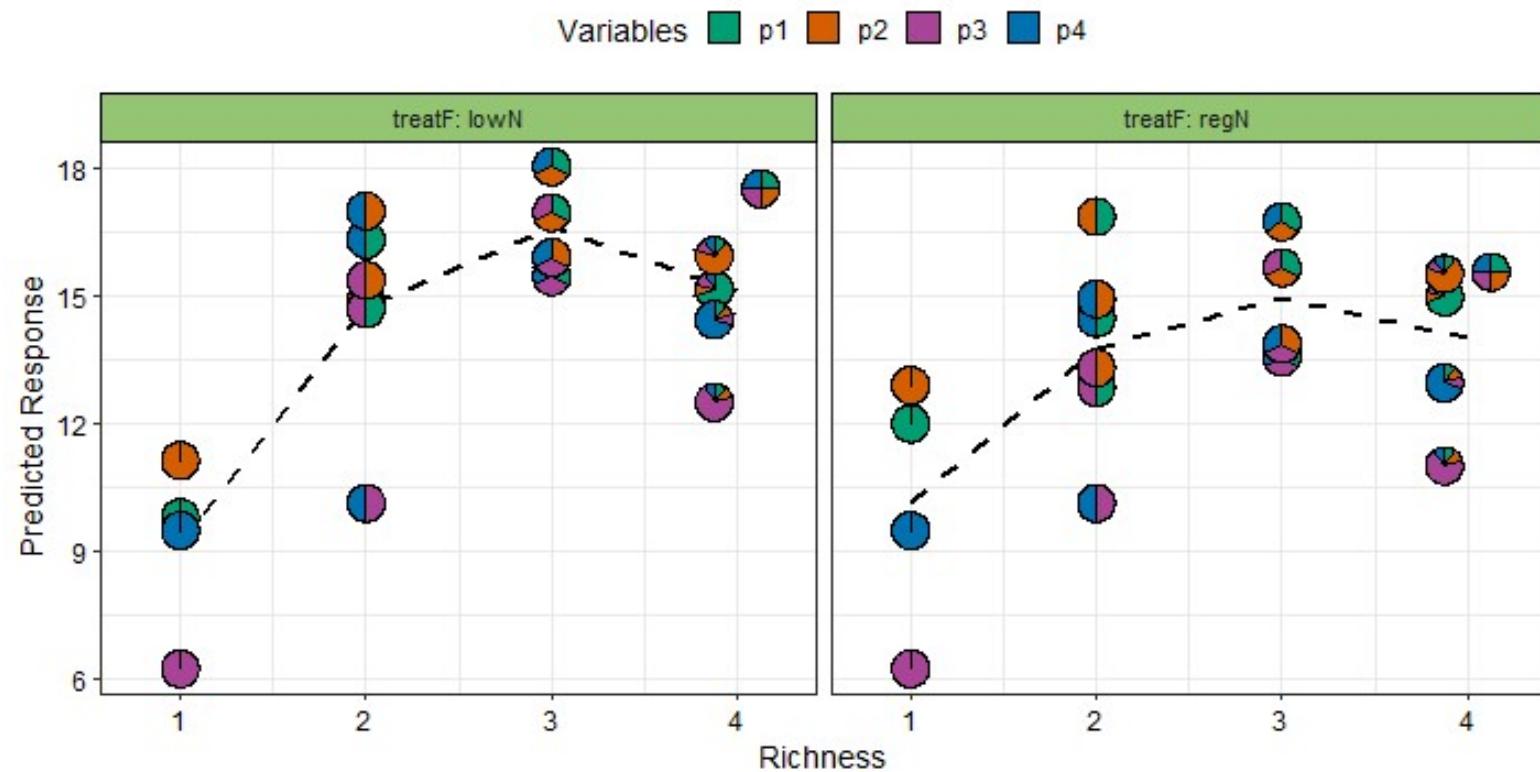
Interpreting the final model



Interpreting the final model

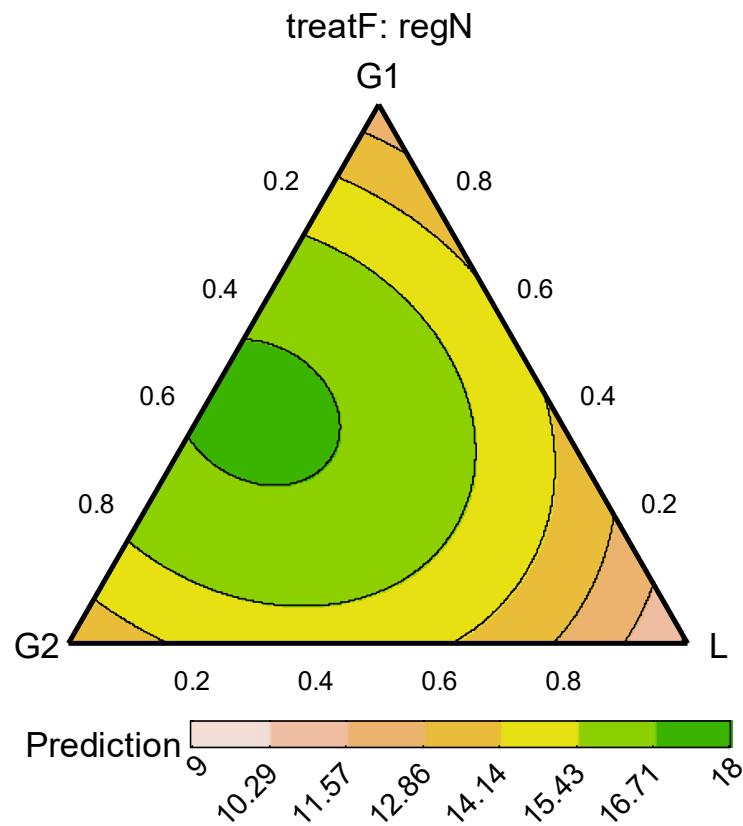
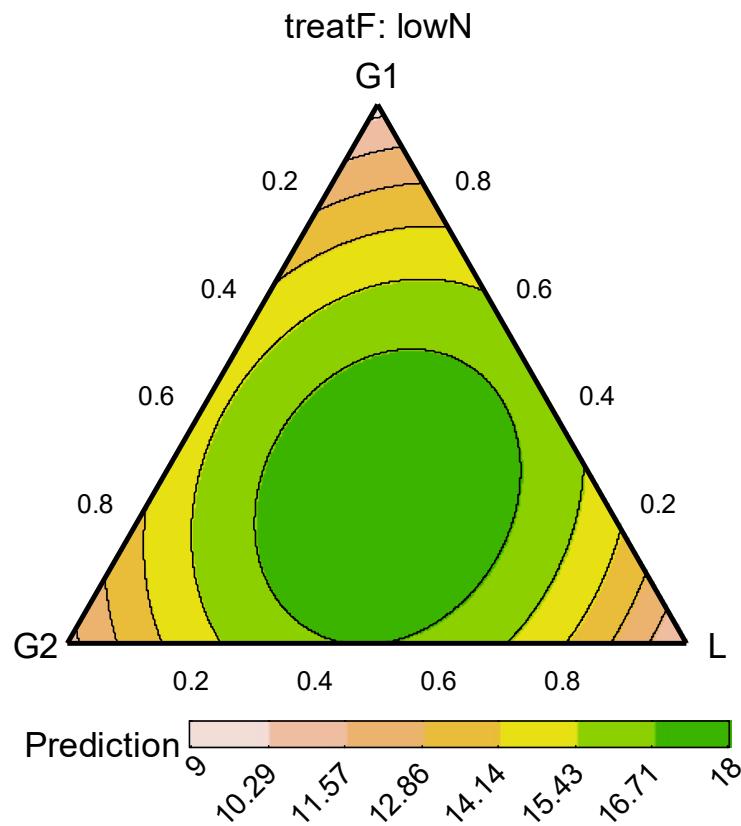


Interpreting the final model



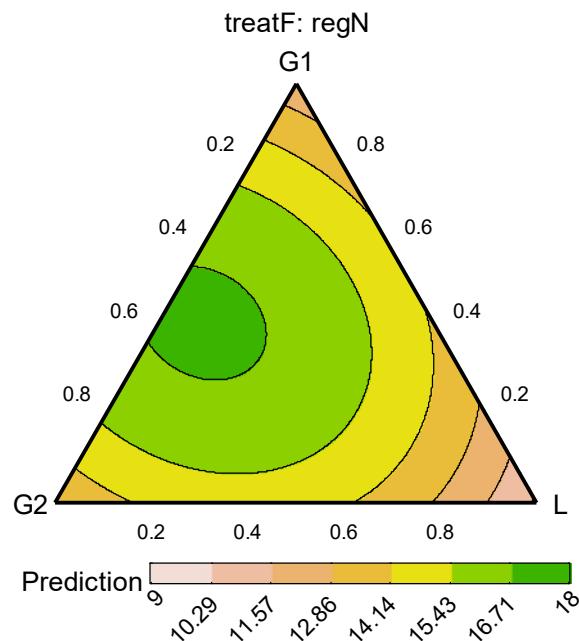
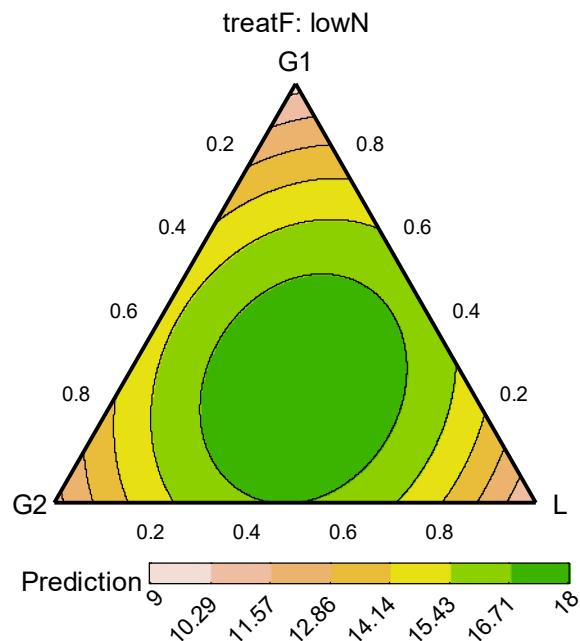
Interpreting the final model

*Each prediction assumes
L1:L2 in an equal ratio*



Interpreting the final model

*Each prediction assumes
L1:L2 in an equal ratio*



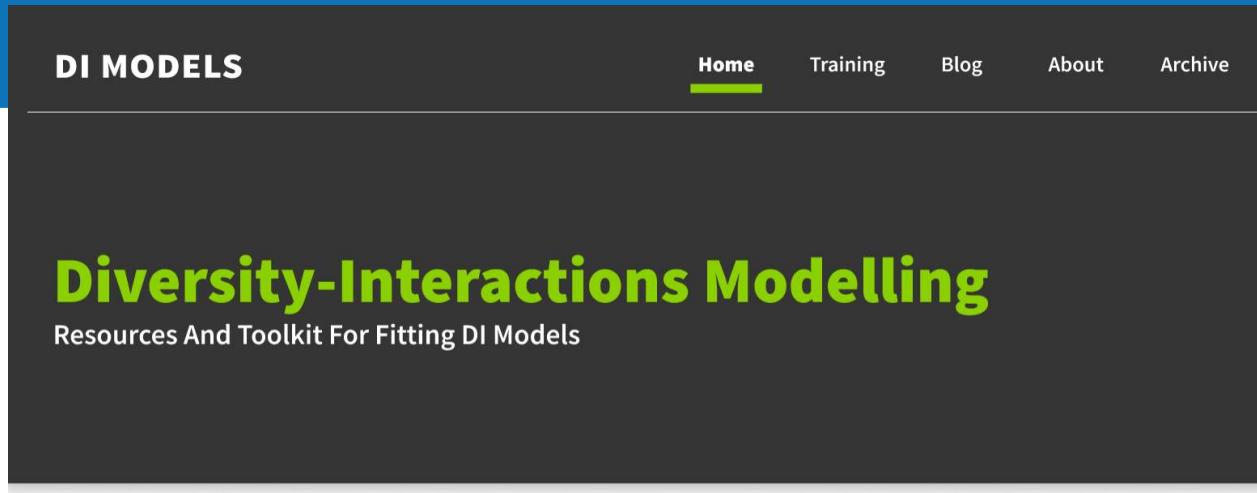
Term	Low N Est	Reg N Est
p1	9.78	11.98
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FG_bfg_GL	26.70	14.92
FG_wfg_G	17.62	17.62
FG_wfg_L	9.05	9.05

Key messages

- Effect of species diversity?
- Effect of low versus regular N fertiliser?
- Other?
- What have you put in your one-page report?

Final remarks

DImodels website



Introduction To Diversity-Interactions Models

Welcome to the Diversity-Interactions (DI) models website! Here you will find out all the latest news and research developments related to DI models. You will also find training resources and guides to fitting and interpreting DI models.

What Is A Diversity-Interactions Model?

In biodiversity and ecosystem function (BEF) studies, usually there are a range of communities varying in species diversity. For example, selecting from a pool of species, the communities may vary in:

- the number of species,
- the identities of the species, and
- the proportions of each species

In a BEF experiment, usually these species diversity variables are manipulated across all experimental units and an ecosystem function is recorded at a later point in time. Models of the BEF relationship assess how species diversity affects an ecosystem function, but should account for all of these variations in species diversity, not just a subset of them. This is what Diversity-Interactions models will do!

DI models jointly assess the effects of species identity, richness, evenness, community composition, and interspecific interactions on an ecosystem function in a regression modelling framework.

The [Dimodels R package](#) is available to implement the Diversity-Interactions modelling approach. Select [Training](#) for advice on how to get started using DI models. Find out all the latest news on our [Blog](#).

References for extending DI models

- Repeated measures and a spatial gradient
 - Kirwan et al (2007) Journal of Ecology 95, 530–539
 - Finn et al (2013) Journal of Applied Ecology 50, 365–375
 - Connolly et al (2018) Journal of Applied Ecology 55, 852-862
- Multivariate responses
 - Dooley et al (2015) Ecology Letters 18, 1242-1251
 - Suter et al (2021) Scientific Reports 11, 1-16
- Dealing with many pairwise interactions
 - Brophy et al (2017) Ecology 98, 1771–1778
- Investigating theta properties
 - Vishwakarma et al (2023) Environmental and Ecological Statistics 30, 555–574.

Packages for fitting and interpreting DI models

`DImodels`, `DImodelsVis`, `DImodelsMulti`.